

Quant II Recitation

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What is this?

- This presentation created using [knitr](#) + [pandoc](#) + [reveal.js](#)
- I have created a recitation repository on github: <https://github.com/ddimmery/Quant-II-Recitation>
- The recitation website will also be on github, at <http://ddimmery.github.io/Quant-II-Recitation>
- This presentation is available on the course website, as is a handout version in pdf.
- The raw .Rmd file is available in the repository. You can create a handout version of it with the following commands (assuming knitr and pandoc are installed), first in R:

```
require(knitr)
knit(presentation.Rmd)
```

- And then on the command line:

```
pandoc presentation.md -o handout.pdf
```

Today's Topic

- Sharing is caring.
 - If you don't share your research (+ code and data) then what's the point of doing it?
- Today we will be discussing some necessary mechanics.
 - R and how to bend it to your will
 - Producing high quality tables / plots
 - If there's any time left, we can talk a little more about identification

Sharing

- All homework will be submitted to me (preferably in hard copy)
- All replication code will be posted to a gist on github, and submitted to me via email.
 - gist.github.com
 - Code should have a header with relevant information (name, date created, date modified, input files, output files, etc)
 - **Code should be well commented**
 - If you'd prefer to submit homework as some sort of knitr document, that is also fine. Just submit the `.Rmd` file.
- All tables and plots should be of very high quality.
- Yes, this will take a non-trivial amount of time.

Workflow

- Find an editor and learn everything about it:
 - **vim** (+ [Vim-R-plugin](#))
 - [emacs](#) (+ [ESS](#) [Emacs Speaks Statistics])
 - [Notepad++](#), [Kate](#), [Sublime](#), etc
 - **Rstudio**
 - [Eclipse](#) (+ [StatET](#))
- Familiarize yourself with version control software
 - [git](#) ([github](#) or [TortoiseGit](#))
 - or just [Dropbox](#)

When things break

- Documentation - Ex: ?1m
- [Google](#)
- CRAN (Reference manuals, vignettes, etc) - Ex: <http://cran.r-project.org/web/packages/AER/index.html>
- JSS - Ex: <http://www.jstatsoft.org/v27/i02>
- Stack Overflow - <http://stackoverflow.com/questions/tagged/r>
- Listservs - <http://www.r-project.org/mail.html>

Resources

- [The Art of R Programming](#) - N. Matloff
- [Modern Applied Statistics with S](#) - W. Venables and B. Ripley
- [Advanced R Programming](#) - forthcoming, H. Wickham
- [The R Inferno](#) - P. Burns
- [Rdataviz](#) - a talk by P. Barberá on ggplot2

Reading R Documentation

- `?lm`

CRAN documentation

- AER

JSS

- `plm`

Confusing Things

- At the prompt, `>` means you're good to go, `+` means a parenthesis or bracket is open.
- Case sensitive
- Use `/` in path names. Not `\`.
- R uses variables – there is no “sheet” here, like in Stata
- **R is a programming language**
- More on errors later!

Using Third-party Code

- Relevant commands are: `install.packages` and `library`
- Find the appropriate packages and commands with Google and via searching in R:

```
?covariance
??covariance
install.packages("sandwich")
library("sandwich")
?vcovHC
```

Data types

- Character - strings
- Double / Numeric - numbers
- Logical - true/false
- Factor - unordered categorical variables
- Objects - its complicated

Character

```
...

str <- "This is a string"

...

paste("This", "is", "a", "string", sep = " ")

## [1] "This is a string"

...

as.character(99)

## [1] "99"

class(str)

## [1] "character"
```

Numeric

```
...  
  
num <- 99.867  
class(num)  
  
## [1] "numeric"  
  
...  
  
round(num, digits = 2)  
  
## [1] 99.87  
  
...  
  
round(str, digits = 2)  
  
## Error: non-numeric argument to mathematical function  
  
...  
  
pi  
  
## [1] 3.142  
  
exp(1)  
  
## [1] 2.718  
  
• sin, exp, log, factorial, choose, BesselJ, etc
```

Logical

```
• The logical type allows us to make statements about truth  
  
...  
  
2 == 4
```

```
## [1] FALSE

class(2 == 4)

## [1] "logical"

...

str != num

## [1] TRUE

...

"34" == 34

## [1] TRUE
```

- ==, !=, >, <, >=, <=, !, &, |, any, all, etc

Objects

- Many functions will return objects rather than a single datatype.

```
...

X <- 1:100
Y <- rnorm(100, X)
out.lm <- lm(Y ~ X)
class(out.lm)

## [1] "lm"

...

out.lm$rank

## [1] 2

class(out.lm$rank)

## [1] "integer"
```

Data Structures

- There are other ways to hold data, though:
 - Vectors
 - Lists
 - Matrices
 - Dataframes

Vectors

- Almost everything in R is a vector.

...

```
as.vector(4)
```

```
## [1] 4
```

```
4
```

```
## [1] 4
```

...

- We can combine vectors with `c`:

...

```
vec <- c("a", "b", "c")
```

```
vec
```

```
## [1] "a" "b" "c"
```

...

```
c(2, 3, vec)
```

```
## [1] "2" "3" "a" "b" "c"
```

Vectors (cont.)

- Sometimes R does some weird stuff:

...

```
c(1, 2, 3, 4) + c(1, 2)
```

```
## [1] 2 4 4 6
```

- It “recycles” the shorter vector:

...

```
c(1, 2, 3, 4) + c(1, 2, 1, 2)
```

```
## [1] 2 4 4 6
```

...

```
c(1, 2, 3, 4) + c(1, 2, 3)
```

```
## Warning: longer object length is not a multiple of shorter object length
```

```
## [1] 2 4 6 5
```

More Vectors

- We can index vectors in several ways

...

```
vec[1]
```

```
## [1] "a"
```

...

```
names(vec) <- c("first", "second", "third")  
vec
```



```
## first second third
## "a" "b" "c"
```

...

```
vec["first"]
```

```
## first
## "a"
```

Missingness

...

```
vec[1] <- NA
vec
```

```
## first second third
## NA "b" "c"
```

...

```
is.na(vec)
```

```
## first second third
## TRUE FALSE FALSE
```

...

```
vec[!is.na(vec)] # vec[complete.cases(vec)]
```

```
## second third
## "b" "c"
```

Lists

- Lists are similar to vectors, but they allow for arbitrary mixing of types and lengths.

...

```

listie <- list(first = vec, second = num)
listie

## $first
## first second third
## NA "b" "c"
##
## $second
## [1] 99.87

...

listie[[1]]

## first second third
## NA "b" "c"

listie$first

## first second third
## NA "b" "c"

```

Matrices

- $A = \begin{pmatrix} 1 & 3 \\ 2 & 4 \end{pmatrix}$
- A_{ij}
- $A_{1,2} = 3$
- $A_{1,\cdot} = (1, 3)$

...

```

A <- matrix(c(1, 2, 3, 4), nrow = 2, ncol = 2)
A

##      [,1] [,2]
## [1,]  1   3
## [2,]  2   4

A[1, 2]

```

```
## [1] 3

A[1, ]

## [1] 1 3
```

Matrix Operations

- Its very easy to manipulate matrices:

```
...

solve(A) #A{-1}

##      [,1] [,2]
## [1,]  -2  1.5
## [2,]   1 -0.5

...

10 * A

##      [,1] [,2]
## [1,]  10  30
## [2,]  20  40

...

B <- diag(c(1, 2))
B

##      [,1] [,2]
## [1,]   1   0
## [2,]   0   2

...

A %*% B

##      [,1] [,2]
## [1,]   1   6
## [2,]   2   8
```

More Matrix Ops.

```
...  
  
A %*% diag(3)  
  
## Error: non-conformable arguments  
  
t(A) # A'  
  
##      [,1] [,2]  
## [1,]    1    2  
## [2,]    3    4  
  
...  
  
rbind(A, B)  
  
##      [,1] [,2]  
## [1,]    1    3  
## [2,]    2    4  
## [3,]    1    0  
## [4,]    0    2  
  
cbind(A, B)  
  
##      [,1] [,2] [,3] [,4]  
## [1,]    1    3    1    0  
## [2,]    2    4    0    2  
  
...  
  
c(1, 2, 3) %x% c(1, 1) # Kronecker Product  
  
## [1] 1 1 2 2 3 3
```

Naming Things

...

```
rownames(A)
```

```
## NULL
```

...

```
rownames(A) <- c("a", "b")
```

```
colnames(A) <- c("c", "d")
```

```
A
```

```
##   c d
```

```
## a 1 3
```

```
## b 2 4
```

...

```
A[, "d"]
```

```
## a b
```

```
## 3 4
```

- Matrices are vectors:

...

```
A[3]
```

```
## [1] 3
```

Dataframes

- The workhorse
- Basically just a matrix that allows mixing of types.

...

```
data(iris)
head(iris)
```

```
##   Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 1         5.1         3.5         1.4         0.2   setosa
## 2         4.9         3.0         1.4         0.2   setosa
## 3         4.7         3.2         1.3         0.2   setosa
## 4         4.6         3.1         1.5         0.2   setosa
## 5         5.0         3.6         1.4         0.2   setosa
## 6         5.4         3.9         1.7         0.4   setosa
```

Control Flow

- loops
- if/else
- functions
- useful stock functions to know

Loops

- for loops - just a way to say “do this for each element of the index”
- “this” is defined in what follows the “for” expression

```
...
```

```
for (i in 1:5) {
  cat(i * 10, " ")
}
```

```
## 10 20 30 40 50
```

```
...
```

```
for (i in 1:length(vec)) {
  cat(vec[i], " ")
}
```

```
## NA b c
```

```
...
```

```
for (i in vec) {  
  cat(i, " ")  
}
```

```
## NA b c
```

If/Else

```
...
```

```
if (vec[2] == "b") print("Hello World!")
```

```
## [1] "Hello World!"
```

```
...
```

```
if (vec[3] == "a") {  
  print("Hello World!")  
} else {  
  print("!dlroW olleH")  
}
```

```
## [1] "!dlroW olleH"
```

Vectorized If/Else

- Conditional execution on each element of a vector

```
...
```

```
vec <- letters[1:3]  
new <- vector(length = length(vec))  
for (i in 1:length(vec)) {  
  if (vec[i] == "b") {  
    new[i] <- 13  
  } else {  
    new[i] <- 0  
  }  
}  
new
```

```
## [1] 0 13 0
...
new <- ifelse(vec == "b", 13, 0)
new
## [1] 0 13 0
```

Functions

- $f : X \rightarrow Y$
- Functions in R are largely the same. (“Pure functions”)

```
...
add3 <- function(X) {
  return(X + 3)
}
add3(2)
## [1] 5
...
makeGroups <- function(groups, members = 1) {
  return((1:groups) %x% rep(1, members))
}
makeGroups(5)
## [1] 1 2 3 4 5
makeGroups(5, 2)
## [1] 1 1 2 2 3 3 4 4 5 5
```


Useful Functions

- Note: Most functions don't do complete case analysis by default (usually option `na.rm=TRUE`)
- `print`, `cat`, `paste`, `with`, `length`, `sort`, `order`, `unique`, `rep`, `nrow`, `ncol`, `complete.cases`, `subset`, `merge`, `mean`, `sum`, `sd`, `var`, `lag`, `lm`, `model.matrix`, `coef`, `vcov`, `residuals`, `vcovHC` (from `sandwich`), `ivreg` (from `AER`), `countrycode` (from `countrycode`), `summary`, `pdf`, `plot`, Tools from `plm`, and many more.

Distributional Functions

- `?Distributions`
- They have a consistent naming scheme.
- `rnorm`, `dnorm`, `qnorm`, `pnorm`
- `rdist` - generate random variable from dist
- `ddist` - density function of dist
- `qdist` - quantile function of dist
- `pdist` - distribution function of dist
- look at documentation for parameterization

...

```
rnorm(16)
```

```
## [1]  0.03219 -0.89729 -0.28782  0.86993 -1.21937  1.47985  0.38488
## [8]  0.28917 -1.66721  0.23155  1.63280  0.84529 -0.87946 -0.22374
## [15]  1.35861 -0.61532
```

Robust SEs

```
1 robust.se <- function(model, cluster=1:length(model$residuals)) {
2   require(sandwich)
3   require(lmtest)
4   M <- length(unique(cluster))
5   N <- length(cluster)
6   K <- model$rank
7   dfc <- (M/(M - 1)) * ((N - 1)/(N - K))
8   uj <- apply(
9     estfun(model),
```

```

10         2,
11         function(x) tapply(x, cluster, sum)
12     )
13     rcse.cov <- dfc * sandwich(model, meat = crossprod(uj)/N)
14     rcse.se <- coeftest(model, rcse.cov)
15     return(list(rcse.cov, rcse.se))
16 }

```

Multiple Dispatch

- Sometimes functions will behave differently based on context:

...

```
summary(vec)
```

```
##      Length      Class      Mode
##           3 character character

```

...

```
summary(c(1, 2, 3, 4))
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      1.00   1.75   2.50   2.50   3.25   4.00

```

...

```
summary(iris[, 1:4])
```

```
##      Sepal.Length  Sepal.Width  Petal.Length  Petal.Width
##      Min.   :4.30  Min.   :2.00  Min.   :1.00  Min.   :0.1
##      1st Qu.:5.10  1st Qu.:2.80  1st Qu.:1.60  1st Qu.:0.3
##      Median :5.80  Median :3.00  Median :4.35  Median :1.3
##      Mean   :5.84  Mean   :3.06  Mean   :3.76  Mean   :1.2
##      3rd Qu.:6.40  3rd Qu.:3.30  3rd Qu.:5.10  3rd Qu.:1.8
##      Max.   :7.90  Max.   :4.40  Max.   :6.90  Max.   :2.5

```

- Why? ?summary ?summary.lm

The *apply family

- These functions allow one to *efficiently* perform a large number of actions on data.
- `apply` - performs actions on the rows or columns of a matrix/array (1 for rows, 2 for columns, 3 for ??)
- `sapply` - performs actions on every element of a vector
- `tapply` - performs actions on a vector by group
- `replicate` - performs the same action a given number of times

apply

```
A
##   c d
## a 1 3
## b 2 4

apply(A, 1, sum)

## a b
## 4 6

apply(A, 2, mean)

##   c   d
## 1.5 3.5
```

sapply

```
vec

## [1] "a" "b" "c"

sapply(vec, function(x) paste0(x, ".vec"))

##      a      b      c
## "a.vec" "b.vec" "c.vec"
```

- Can be accomplished more simply with:

...

```
paste0(vec, ".vec")
```

```
## [1] "a.vec" "b.vec" "c.vec"
```

- Why?
- `replicate` is basically just `sapply(1:N,funct)` where `funct` never uses the index.

tapply

```
tapply(1:10, makeGroups(5, 2), mean)
```

```
##  1  2  3  4  5  
## 1.5 3.5 5.5 7.5 9.5
```

Working With Data

- Input
- Output

Input

...

```
setwd("~/github/Quant II Recitation/2014-01-31/")  
dir()
```

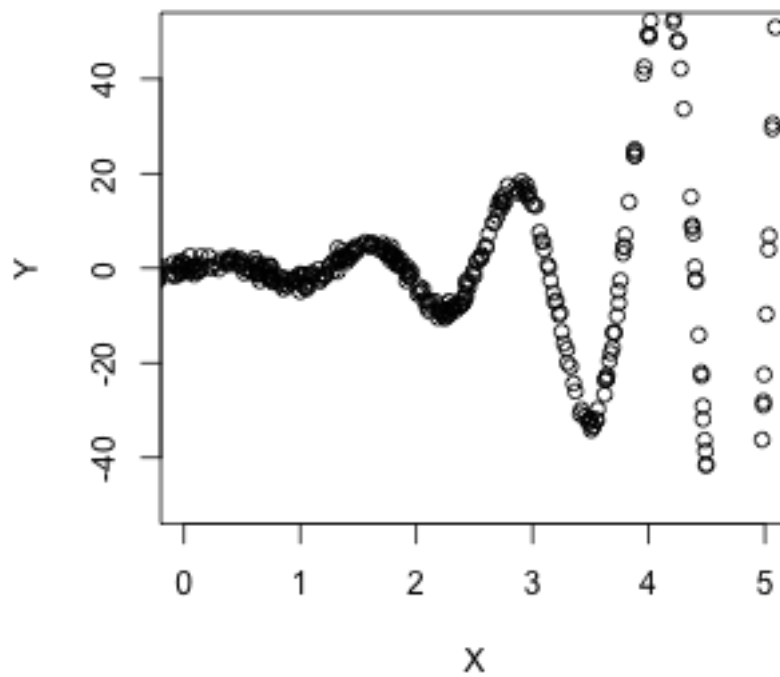
```
## [1] "apsrtable.png"      "figure"           "handout.pdf"  
## [4] "iris.csv"            "presentation.html" "presentation.md"  
## [7] "presentation.Rmd"    "stargazer.png"
```

```
iris <- read.csv("iris.csv")
```

- If data is, for instance, a Stata `.dta` file, use `read.dta` from the `foreign` package.
- Useful options for reading data: `sep`, `na.strings`, `stringsAsFactors`
- For different formats, Google it.

Simulate some Data

```
set.seed(1023) # Important for replication
X <- rnorm(1000, 0, 5)
Y <- sin(5 * X) * exp(abs(X)) + rnorm(1000)
dat <- data.frame(X, Y)
plot(X, Y, xlim = c(0, 5), ylim = c(-50, 50))
```



Regression Output

```
dat.lm <- lm(Y ~ X, data = dat)
dat.lm

##
```

```
## Call:
## lm(formula = Y ~ X, data = dat)
##
## Coefficients:
## (Intercept)          X
##    -216634         183687
```

Regression Output

```
summary(dat.lm)
```

```
##
## Call:
## lm(formula = Y ~ X, data = dat)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.10e+08 -4.19e+05  2.01e+05  8.17e+05  9.08e+06
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -216634     212126  -1.02   0.31
## X            183687     43470    4.23  2.6e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6710000 on 998 degrees of freedom
## Multiple R-squared:  0.0176, Adjusted R-squared:  0.0166
## F-statistic: 17.9 on 1 and 998 DF,  p-value: 2.6e-05
```

Pretty Output

- How do we get LaTeX output?
- The xtable package:

...

```
require(xtable)
```

```
## Loading required package: xtable
```

```
xtable(dat.lm)
```

```

## % latex table generated in R 3.0.2 by xtable 1.7-1 package
## % Tue Jan 28 23:38:40 2014
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrrrr}
## \hline
## & Estimate & Std. Error & t value & Pr(>$$|t$|$) \\\
## \hline
## (Intercept) & -216633.6722 & 212125.4622 & -1.02 & 0.3074 \\\
## X & 183687.1735 & 43469.5839 & 4.23 & 0.0000 \\\
## \hline
## \end{tabular}
## \end{table}

```

xtable

- xtable works on any sort of matrix

...

`xtable(A)`

```

## % latex table generated in R 3.0.2 by xtable 1.7-1 package
## % Tue Jan 28 23:38:40 2014
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrr}
## \hline
## & c & d \\\
## \hline
## a & 1.00 & 3.00 \\\
## b & 2.00 & 4.00 \\\
## \hline
## \end{tabular}
## \end{table}

```

xtable

- This is what xtable does with the `lm` object:

...

```

class(summary(dat.lm)$coefficients)

## [1] "matrix"

xtable(summary(dat.lm)$coefficients)

## % latex table generated in R 3.0.2 by xtable 1.7-1 package
## % Tue Jan 28 23:38:40 2014
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrrrr}
## \hline
## & Estimate & Std. Error & t value & Pr(>$$|t$|)$ \\
## \hline
## (Intercept) & -216633.67 & 212125.46 & -1.02 & 0.31 \\
## X & 183687.17 & 43469.58 & 4.23 & 0.00 \\
## \hline
## \end{tabular}
## \end{table}

```

- Note that this is the same as the output from `xtable(dat.lm)`

Pretty it up

- Now let's make some changes to what `xtable` spits out:

```

...

print(xtable(dat.lm, digits = 1), booktabs = TRUE)

## % latex table generated in R 3.0.2 by xtable 1.7-1 package
## % Tue Jan 28 23:38:40 2014
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrrrr}
## \toprule
## & Estimate & Std. Error & t value & Pr(>$$|t$|)$ \\
## \midrule
## (Intercept) & -216633.7 & 212125.5 & -1.0 & 0.3 \\
## X & 183687.2 & 43469.6 & 4.2 & 0.0 \\
## \bottomrule
## \end{tabular}
## \end{table}

```

- Many more options, see `?xtable` and `?print.xtable`

apsrtable

- Read the documentation - there are many options.

```
require(apsrtable)

## Loading required package: apsrtable

dat.lm2 <- lm(Y ~ X + 0, data = dat)
apsrtable(dat.lm, dat.lm2)

## Note: no visible binding for global variable 'se'
## Note: no visible binding for global variable 'se'
## Note: no visible binding for global variable 'nmodels'
## Note: no visible binding for global variable 'lev'

## \begin{table}[!ht]
## \caption{}
## \label{}
## \begin{tabular}{l D{.}{.}{2}D{.}{.}{2} }
## \hline
## & \multicolumn{1}{c}{ Model 1 } & \multicolumn{1}{c}{ Model 2 } \\ \hline
## % & Model 1 & Model 2 & \\
## (Intercept) & -216633.67 & & \\
## & (212125.46) & & \\
## X & 183687.17 ^* & 182921.71 ^* \\
## & (43469.58) & (43464.06) & \\
## $N$ & 1000 & 1000 & \\
## $R^2$ & 0.02 & 0.02 & \\
## adj. $R^2$ & 0.02 & 0.02 & \\
## Resid. sd & 6706998.86 & 6707143.05 & \\ \hline
## \multicolumn{3}{l}{\footnotesize{Standard errors in parentheses}} \\
## \multicolumn{3}{l}{\footnotesize{^* indicates significance at $p < 0.05$}}
## \end{tabular}
## \end{table}
```

apsrtable

```
library(png)
library(grid)
img <- readPNG("apsrtable.png")
grid.raster(img)
```

	Model 1	Model 2
(Intercept)	-216633.67 (212125.46)	
X	183687.17* (43469.58)	182921.71* (43464.06)
N	1000	1000
R^2	0.02	0.02
adj. R^2	0.02	0.02
Resid. sd	6706998.86	6707143.05

Standard errors in parentheses

* indicates significance at $p < 0.05$

stargazer

```
require(stargazer)
```

```
## Loading required package: stargazer
```

```
##
```

```
## Please cite as:
```

```
##
```

```
## Hlavac, Marek (2013). stargazer: LaTeX code and ASCII text for well-formatted regression
```

```
## R package version 4.5.3. http://CRAN.R-project.org/package=stargazer
```

```
stargazer(dat.lm, dat.lm2)
```

```
##
```

```
## % Table created by stargazer v.4.5.3 by Marek Hlavac, Harvard University. E-mail: hlavac
```

```
## % Date and time: Tue, Jan 28, 2014 - 23:38:48
```

```
## \begin{table}[!htbp] \centering
```

```
## \caption{}
```

```
## \label{}
```

```
## \begin{tabular}{@{\extracolsep{5pt}}lcc}
```

```
## \hline
```

```
## \hline \hline
```

```
## & \multicolumn{2}{c}{\textit{Dependent variable:}} \hline
```

```
## \cline{2-3}
```

```
## \hline & \multicolumn{2}{c}{Y} \hline
```

```
## \hline & (1) & (2) \hline
```

```
## \hline \hline
```

```
## X & 183,687.000*** & 182,922.000*** \hline
```

```
## & (43,470.000) & (43,464.000) \hline
```

```
## & & \hline
```

```
## Constant & $-216,634.000 & \hline
```

```
## & (212,125.000) & \hline
```

```
## & & \hline
```

```
## \hline \hline
```

```
## Observations & 1,000 & 1,000 \hline
```

```
## R2 & 0.018 & 0.017 \hline
```

```
## Adjusted R2 & 0.017 & 0.016 \hline
```

```
## Residual Std. Error & 6,706,999.000 (df = 998) & 6,707,143.000 (df = 999) \hline
```

```
## F Statistic & 17.860*** (df = 1; 998) & 17.710*** (df = 1; 999) \hline
```

```
## \hline
```

```
## \hline \hline
```

```
## \textit{Note:} & \multicolumn{2}{r}{*$p<$0.1; **$p<$0.05; ***$p<$0.01} \hline
```

```
## \normalsize
```

```
## \end{tabular}
```

```
## \end{table}
```

stargazer

```
img <- readPNG("stargazer.png")  
grid.raster(img)
```

	<i>Dependent variable:</i>	
	Y	
	(1)	(2)
X	183,687.200*** (43,469.580)	182,921.700*** (43,464.060)
Constant	-216,633.700 (212,125.500)	
Observations	1,000	1,000
R ²	0.018	0.017
Adjusted R ²	0.017	0.016
Residual Std. Error	6,706,999.000 (df = 998)	6,707,143.000 (df = 999)
F Statistic	17.856*** (df = 1; 998)	17.712*** (df = 1; 999)

Note: *p<0.1; **p<0.05; ***p<0.01

Both

- Both packages are good (and can be supplemented with `xtable` when it is easier)
- Get pretty close to what you want with these packages, and then tweak the LaTeX directly.

Plotting

- It's all about coordinate pairs.
- `plot(x,y)` plots the pairs of points in `x` and `y`
- Notable options:
 - `type` - determines whether you plot points, lines or whatnot
 - `pch` - determines plotting character
 - `xlim` - x limits of the plot (likewise for `y`)
 - `xlab` - label on the x-axis
 - `main` - main plot label
 - `col` - color
 - A massive number of options. Read the docs.
- Some objects respond specially to `plot`. Try `plot(dat.lm)`

Tying it Together

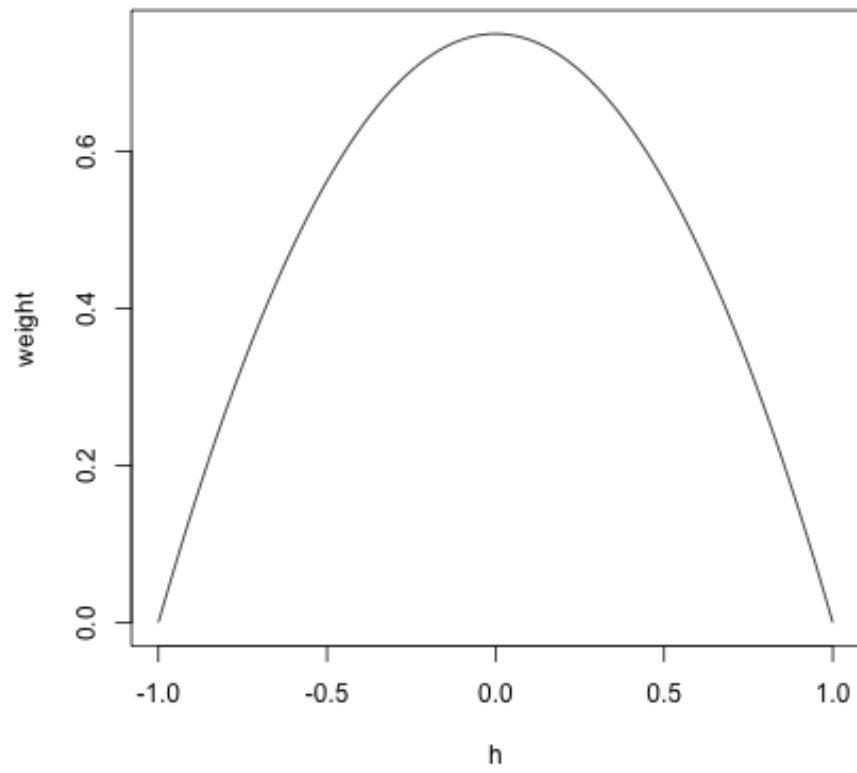
```
x <- seq(-1, 1, 0.01)
y <- 3/4 * (1 - x^2)
plot(x, y, type = "l", xlab = "h", ylab = "weight")
```

Tying it Together

- W is an $n \times p$ diagonal weighting matrix, h is a “bandwidth”.
- Diagonal entries are $\frac{3}{4} \cdot (1 - d^2) \cdot 1_{\{|d| \leq 1\}}$ where $d = \frac{X-c}{h}$
- $\hat{\beta}_c = (X'WX)^{-1}X'WY$
- Covariance matrix is $s^2(X'WX)^{-1}$

...

```
loc.lin <- function(Y, X, c = 0, bw = sd(X)/2) {
  d <- (X - c)/bw
  W <- 3/4 * (1 - d^2) * (abs(d) < 1)
  W <- diag(W)
  X <- cbind(1, d)
  b <- solve(t(X) %*% W %*% X) %*% t(X) %*% W %*% Y
  sigma <- t(Y - X %*% b) %*% W %*% (Y - X %*% b) / (sum(diag(W) > 0) - 2)
  sigma <- solve(t(X) %*% W %*% X) * c(sigma)
  return(c(est = b[1], se = sqrt(diag(sigma))[1]))
}
```



Fit the Surface

```
X.est <- seq(0, 5, 0.1)
dat.llm <- sapply(X.est, function(x) loc.lin(Y, X, c = x, bw = 0.25))
plot(X, Y, xlim = c(0, 5), ylim = c(-50, 50), pch = 20)
lines(X.est, dat.llm[1, ], col = "red")
lines(X.est, dat.llm[1, ] + 1.96 * dat.llm[2, ], col = "pink")
lines(X.est, dat.llm[1, ] - 1.96 * dat.llm[2, ], col = "pink")
```

